بر ای دسترسی به نسخه کامل حل المسائل، روی لینک زیر کلیک کنید و یا به وبسایت "ایبوک یاب" مراجعه بفر مایید Email: ebookyab.ir@gmail.com, Phone:+989359542944 (Telegram, WhatsApp, Eitaa) https://ebookyab.ir/solution-manual-principles-of-foundation-engineering-braja-das/

Chapter 2

- 2.1 From Eq. (2.18), $\rho_d = \frac{G_s \rho_w}{1+e} = \frac{2450}{0.925} = \frac{2.80 \times 1000}{1+e} ; e = 0.0571$ From Eq. (2.6), Porosity, $n = \frac{e}{1+e} = \frac{0.0571}{1+0.0571} = 0.054$
- 2.2 From Eq. (2.13), the dry density

$$\rho_d = \frac{\rho}{1+w} = \frac{2060}{1+0.153} = 1786.6 \text{ kg/m}^3$$

From Eq. (2.18), $\rho_d = \frac{G_s \rho_w}{1+e}$

$$e = \frac{G_s \rho_w}{\rho_d} - 1 = \frac{2.70 \times 1000}{1786.6} - 1 = 0.511$$

Once saturated, from Eq. (2.19),

$$\rho_{\text{sat}} = \frac{(G_s + e)}{(1 + e)} \rho_w = \frac{(2.70 + 0.511)}{(1 + 0.511)} \times 1000 = 2125.1 \text{ kg/m}^3$$

2.3 Let's consider a 1-m² area in plan. The initial volume of this soil is $V = 1 \times 0.5 = 0.5 \text{ m}^3$. Volume of the solids is V_s .

$$e = 0.9 = \frac{0.5 - V_s}{V_s}$$
; $V_s = 0.2632 \text{ m}^3$

$$W_s = 0.2632 \times 2.68 \times 9.81 = 6.919 \text{ kN}$$

The new volume after compaction = $1 \times 0.455 = 0.455 \text{ m}^3$

The dry unit weight, $\gamma_d = \frac{6.919}{0.455} = 15.21 \text{ kN/m}^3$

From Eq. (2.12), $\gamma_d = \frac{G_s \gamma_w}{1+e}$

$$e = \frac{G_s \gamma_w}{\gamma_d} - 1 = \frac{2.68 \times 9.81}{15.21} - 1 = 0.729$$

From Eq. (2.13), $\gamma = (15.21)(1+0.20) = 18.25 \text{ kN/m}^3$

2.4 At the compacted road base, the weight of solids, $W_s = 120,000 \times 19.5 = 2,340,000 \text{ kN}$

At the borrow pit, the dry unit weight, $\gamma_d = \frac{\gamma}{1+w} = \frac{17.5}{1+0.085} = 16.13 \text{ kN/m}^3$

Volume of the pit, $V = \frac{2,340,000}{16.13} = 145,080 \text{ m}^3$

The moisture content has to be increased from 8.5% (at the borrow pit) to 14.0% (at the road base). The quantity of water to add,

2,340,000 × (0.14 – 0.085) = 128,700 kN Volume of water to be added = $\frac{128,700}{9.81}$ = 13,119.3 m³

- 2.5 $\gamma_d = \frac{\gamma}{1+w} = \frac{110.4}{1+0.105} = 99.9 \text{ lb/ft}^3$ $\gamma_d = \frac{G_s \gamma_w}{1+e}; \ e = \frac{2.65 \times 62.4}{99.9} - 1 = 0.655$ From Eq. (2.23), $D_r = \frac{0.870 - 0.655}{0.870 - 0.515} \times 100 = 60.6\%$
- 2.6 a. A-1-a c. A-3 b. A-1-b d. A-7-6

2.7 Soil A: % of gravel = 50, % of sand = 13, % of fines = 37 $D_{10} = 0.035 \text{ mm}, D_{30} = 0.061 \text{ mm}, D_{60} = 9.8 \text{ mm} \rightarrow C_u = 280; C_c = 0.02$ $LL = 58, PL = 34, PI = 24 \rightarrow \text{plots below the A-line; hence, silt}$ The soil can be described as **poorly (gap) graded sandy silty gravel**

with a group symbol of GM.

Soil B: % of gravel = 24, % of sand = 69, % of fines = 7

$$D_{10} = 0.17 \text{ mm}, D_{30} = 0.82 \text{ mm}, D_{60} = 2.6 \text{ mm} \rightarrow C_u = 15.3; C_c = 1.5$$

 $LL = 42, PL = 22, PI = 20 \rightarrow \text{plots above the A-line; hence, clay}$
The soil can be described as well graded clayey gravelly sand with a

Soil C: % of gravel = 1, % of sand = 99, % of fines = 0 $D_{10} = 0.7 \text{ mm}, D_{30} = 1.2 \text{ mm}, D_{60} = 1.6 \text{ mm} \rightarrow C_u = 2.3; C_c = 1.3$ The soil can be described as **poorly (uniformly) graded sand with a**

group symbol of SW-SM.

group symbol of SP.

Soil D: % of gravel = 0, % of sand = 12, % of fines = 88 LL = 75, PL = 31, PI = 44 → plots above the A-line; hence, clay. The soil can be described as sandy clay of high plasticity with a group symbol of CH.

2.8 The head loss from the reservoir to the ditch, $\Delta h = 38 - 28 = 10.0 \text{ m}$ The length of the sand seam in the direction of the flow, $L = 200/\cos 10 = 203.1 \text{ m}$ The hydraulic gradient, i = 10.0/203.1 = 0.0492By Darcy's law [Eq. (2.35)], $v = (2.6 \times 10^{-5} \text{ m/s})(0.0492) = 0.128 \times 10^{-5} \text{ m/s}$ The cross section of the sand seam through which the flow takes place is $1.0 \times 500.0 = 500.0 \text{ m}^2$ The flow rate = $(0.128 \times 10^{-5} \text{ m/s})(500.0 \text{ m}^2) = 64.0 \times 10^{-5} \text{ m}^3/\text{s}$ Volume of water flowing into the ditch per day: $= (64.0 \times 10^{-5} \text{ m}^3/\text{s})(24)(3600) = 55.3 \text{ m}^3$

2.9 For the flow net shown in Figure P2.9, $N_f = 3$ and $N_d = 10$ Total head loss from right to left, $h_{max} = 5.0$ m The flow rate is given by [Eq. (2.46)]

$$q = kh_{\text{max}} \frac{N_f}{N_d} = (1.5 \times 10^{-5})(5.0) \left(\frac{3}{10}\right) = 2.25 \times 10^{-5} \text{ m}^3/\text{s/m length}$$
$$= (2.25 \times 10^{-5})(50.0)(24)(3600 \text{ m}^3/\text{day}) = 97.2 \text{ m}^3/\text{day}$$

- 2.10 On top of the soft clay layer (i.e., at 10 m depth), initially: $\sigma' = 1 \times 17.0 + 9(20 - 9.81) = 108.7 \text{ kN/m}^2$ After the water table is lowered, $\sigma' = 3 \times 17.0 + 7(20 - 9.81) = 122.3 \text{ kN/m}^2$ By lowering the water table, the effective stress has increased by (122.3 - 108.7) = 13.6 kN/m²
- 2.11 The soil below the water table can be assumed to be fully saturated (i.e., S = 1). $e = wG_s = 0.25 \times 2.70 = 0.675$

The saturated unit weight can be computed as

$$\gamma_{\text{sat}} = \frac{(G_s + e)\gamma_w}{1 + e} = \frac{(2.70 + 0.675) \times 9.81}{1 + 0.675} = 19.8 \text{ kN/m}^3$$

At a depth of 5 m into the sandy clay,

 $\sigma = 4 \times 9.81 + 5 \times 19.8 = 138.3 \text{ kN/m}^2$ $u = 9 \times 9.81 = 88.3 \text{ kN/m}^2$ $\sigma' = \sigma - u = 138.3 - 88.3 = 50 \text{ kN/m}^2$

2.12 Refer to the figure.



a. The compression index C_c is given by [Eq. (2.53)],

$$C_c = \frac{e_1 - e_2}{\log \sigma_2' - \log \sigma_1'} = \frac{1.10 - 0.85}{\log 240 - \log 65} = 0.441$$

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b. Let the void ratio at 460 kN/m² pressure be e_3 .

$$e_1 - e_3 = C_c (\log 460 - \log 65) = 0.441 \times \log \left(\frac{460}{65}\right) = 0.375$$

 $e_3 = 1.10 - 0.375 = 0.725$

2.13 a. The clay is below the water table and, hence, is saturated. The initial void ratio e_o can be determined as

$$e_o = wG_s = 0.225 \times 2.72 = 0.612$$

The saturated unit weight is determined as

$$\gamma_{\text{sat}} = \frac{(G_s + e)\gamma_w}{1 + e} = \frac{(2.72 + 0.612)(9.81)}{1 + 0.612} = 20.3 \text{ kN/m}^3$$

The effective overburden stress at the middle of the clay is

$$\sigma'_{o} = 2 \times 17.0 + 3(20.2 - 9.81) + 1.5(20.3 - 9.81) = 80.3 \text{ kN/m}^{2} < 110.0 \text{ kN/m}^{2}$$

Since the preconsolidation pressure is greater than the current overburden pressure, the **clay is overconsolidated**. The overconsolidation ratio

$$OCR = 110.0/80.3 = 1.37$$

b. The 2-m-high compacted fill imposes a surcharge of $2 \times 20 = 40 \text{ kN/m}^2$ (i.e., $\Delta \sigma' = 40.0 \text{ kN/m}^2$, $\sigma'_o = 80.3 \text{ kN/m}^2$, and $\sigma'_c = 110.0 \text{ kN/m}^2$)

Since $\sigma'_o + \Delta \sigma' > \sigma'_c$, the consolidation settlement can be computed from Eq. (2.69) as

$$S_{p} = \frac{C_{s}H}{1+e_{o}}\log\left(\frac{\sigma_{c}'}{\sigma_{o}'}\right) + \frac{C_{c}H}{1+e_{o}}\log\left(\frac{\sigma_{o}'+\Delta\sigma'}{\sigma_{c}'}\right)$$
$$= \frac{0.06 \times 3000}{1+0.612}\log\left(\frac{110.0}{80.3}\right) + \frac{0.52 \times 3000}{1+0.612}\log\left(\frac{80.3+40.0}{110}\right)$$
$$= 52.9 \text{ mm}$$

2.14 For U = 75%, $T_v = 0.477$ (Table 2.12)

$$T_{v} = \frac{c_{v}t}{H_{\rm dr}^2}$$

From two-way (doubly drained) to one-way (singly drained), H_{dr} is doubled. For the same U and, hence, the same T_{ν} , this would increase the time fourfold. Therefore, it will take **4t years**.

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2.15 a. The clay layer with one-way drainage has H_c of 6.0 m. After one year,

$$T_v = \frac{c_v t}{H^2} = \frac{0.0014 \times 365 \times 24 \times 3600}{600^2} = 0.123$$
; settlement, $S_{c(t)} = 160$ mm

From Table 2.12, U = 39.6%

$$U = \frac{S_{c(t)}}{S_{c(max)}}$$
; $S_{c(max)} = 160/0.396 = 404 \text{ mm}$

When t = 2 years, $T_v = 0.246$.

From Table 2.12, U = 55.8%.

Consolidation settlement during the first two years is $0.558 \times 404 = 225.4$ mm

b. The initial effective overburden stress at the middle of the clay is $\sigma'_{o} = 1.5 \times 17.0 + 0.5(18.5 - 9.81) + 3.0(19.0 - 9.81) = 57.4 \text{ kN/m}^{2}$ $\Delta \sigma' = 3 \times 19 = 57 \text{ kN/m}^{2}$ $S_{c} = \frac{C_{c}H}{1 + e_{o}} \log \left(\frac{\sigma'_{o} + \Delta \sigma'}{\sigma'_{o}}\right)$ $404 = \frac{C_{c} \times 6000}{1 + 0.810} \log \left(\frac{57.4 + 57.0}{57.4}\right); \quad C_{c} = 0.41$

2.16 a. For the clay layer, assuming S = 100% below the water table, $e_o = 0.45 \times 2.70 = 1.215$

$$\gamma_{\text{sat}} = \frac{(G_s + e)\gamma_w}{1 + e} = \frac{(2.70 + 1.215) \times 9.81}{1 + 1.215} = 17.3 \text{ kN/m}^3$$

The initial effective overburden stress at the middle of the clay layer is

$$\sigma'_{o} = 1 \times 16 + 1(19.0 - 9.81) + 1.5(17.3 - 9.81) = 36.4 \text{ kN/m}^{2}$$

With OCR = 1.5, the preconsolidation pressure $\sigma'_c = 1.5 \times 36.4 = 54.6 \text{ kN/m}^2$

When the fill is placed, it imposes a surcharge of $\Delta \sigma' = 20 \times 1.5 = 30.0 \text{ kN/m}^2$ From Eq. (2.69),

$$S_{c} = \frac{C_{s}H}{1+e_{o}}\log\left(\frac{\sigma_{c}'}{\sigma_{o}'}\right) + \frac{C_{c}H}{1+e_{o}}\log\left(\frac{\sigma_{o}'+\Delta\sigma'}{\sigma_{c}'}\right)$$
$$= \frac{0.08\times3000}{1+1.215}\log\left(\frac{54.6}{36.4}\right) + \frac{0.65\times3000}{1+1.215}\log\left(\frac{66.4}{54.6}\right) = 93.9 \text{ mm}$$

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b. Including the fill load and the warehouse load, $\Delta \sigma' = 30 + 40 = 70 \text{ kN/m}^2$

$$S_{c} = \frac{C_{s}H}{1+e_{o}}\log\left(\frac{\sigma_{c}'}{\sigma_{o}'}\right) + \frac{C_{c}H}{1+e_{o}}\log\left(\frac{\sigma_{o}'+\Delta\sigma'}{\sigma_{c}'}\right)$$
$$= \frac{0.08\times3000}{1+1.215}\log\left(\frac{54.6}{36.4}\right) + \frac{0.65\times3000}{1+1.215}\log\left(\frac{106.4}{54.6}\right)$$
$$= 274.2 \text{ mm}$$

Consolidation settlement due to the warehouse alone is 274.2 - 93.9 = 180.3 mm

2.17 The direct shear test data are plotted in the figure. From the failure envelope, $c' = 6.5 \text{ kN/m}^2 \text{ and } \phi' = \tan^{-1}(0.4292) = 23.2^{\circ}$



2.18 a. $\sigma'_3 = 100 \text{ kN/m}^2 \text{ and } \Delta \sigma_f = 260 \text{ kN/m}^2$

Therefore, $\sigma'_1 = \sigma'_3 + \Delta \sigma_f = 360 \text{ kN/m}^2$

From Eq. (2.91),
$$\sigma'_1 = \sigma'_3 \tan^2 \left(45 + \frac{\phi'}{2} \right) + 2c' \tan \left(45 + \frac{\phi'}{2} \right)$$

For normally consolidated clays, c' = 0; hence,

$$360 = 100 \tan^2 \left(45 + \frac{\phi'}{2} \right); \ \phi' = 34.4^\circ$$

b. For the second specimen,
$$\sigma'_3 = 200 \text{ kN/m}^2$$

$$\sigma_1' = 200 \tan^2 \left(45 + \frac{34.4}{2} \right) = 719.5 \text{ kN/m}^2$$
$$\Delta \sigma_f = 719.5 - 200 = 519.5 \text{ kN / m}^2$$

2.19 a. In normally consolidated clay,
$$c' = 0$$

For the first specimen (consolidated drained test), using Eq. (2.91),

$$260 + 150 = 410 = 150 \tan^2 \left(45 + \frac{\phi'}{2} \right); \ \phi' = 27.7^\circ$$

In the second specimen (consolidated undrained test), applying the same value of ϕ' in Eq. (2.91),

$$\sigma_{3} = 150 \text{ kN/m}^{2} \text{ and } \Delta \sigma_{f} = 115 \text{ kN/m}^{2}$$

$$\sigma_{1} = \sigma_{3} + \Delta \sigma_{f} = 265 \text{ kN/m}^{2}$$

$$\sigma_{3}' = 150 - u_{f} \text{ and } \sigma_{1}' = 265 - u_{f}$$

$$\sigma_{1}' = \sigma_{3}' \tan^{2} \left(45 + \frac{\phi'}{2} \right) = \sigma_{3}' \tan^{2} \left(45 + \frac{27.7}{2} \right) = 2.737 \sigma_{3}'$$

$$265 - u_{f} = (150 - u_{f}) \times 2.737; \ u_{f} = 83.8 \text{ kN/m}^{2}$$

b. From Eq. (2.96),
$$A_f = \frac{u_f}{\Delta \sigma_f} = \frac{83.8}{115} = 0.73$$

2.20 At failure the pore water pressure is u_f , $\sigma_3 = 100 \text{ kN/m}^2$ and $\sigma_1 = 207 \text{ kN/m}^2$. $\sigma'_3 = 100 - u_f$ and $\sigma'_1 = 207 - u_f$ Substituting for σ'_3 and σ'_1 in Eq. (2.91), $\sigma'_1 = \sigma'_3 \tan^2 \left(45 + \frac{\phi'}{2} \right) + 2c' \tan \left(45 + \frac{\phi'}{2} \right)$ $\left(207 - u_f \right) = \left(100 - u_f \right) \tan^2 \left(45 + \frac{26}{2} \right) + 2 \times 10 \tan \left(45 + \frac{26}{2} \right)$ $u_f = 51.9 \text{ kN/m}^2$

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2.21 The following table can be prepared from the given data, and the Mohr circles are plotted as shown in the figure.

Sample No.	σ_3 (kN/m ²)	$(\Delta \sigma_d)_f$ (kN/m ²)	$(\Delta u_d)_f$ (kN/m ²)	σ_1 (kN/m ²)	σ'_3 (kN/m ²)	σ'_1 (kN/m ²)
1	100	88.2	57.4	188.2	42.6	130.8
2	200	138.5	123.7	338.5	76.3	214.8
3	350	232.1	208.8	582.1	141.2	373.3



The failure envelope is drawn tangent to the Mohr circles in the figure and, from measurements, $c' = 10.0 \text{ kN/m}^2$ and $\phi' = 24.7^\circ$

2.22 The unconfined compressive strength of the clay specimen $q_u = 2c_u = 90 \text{ kN/m}^2$ Cross sectional area of the specimen $= \frac{\pi}{4} \times 75^2 = 4417.9 \text{ mm}^2$ Maximum load the specimen can carry $= 90 \times 4417.9 \times 10^{-6} = 0.398 \text{ kN} = 398 \text{ N}$ Weight of one steel plate $= 1.5 \times 9.81 \text{ N} = 7.358 \text{ N}$ Therefore, number of plates that can be stacked on the specimen = 398/7.358 = 54With $q_u = 90 \text{ kN/m}^2$ (see Table 2.14), it is a **medium clay** (consistency).

2.23 a. From Figure P2.7,
$$D_{10} = 0.7$$
 mm, $D_{15} = 0.9$ mm, $D_{30} = 1.2$ mm,

$$D_{50} = 1.4 \text{ mm}, D_{60} = 1.6 \text{ mm}, \text{ and } D_{85} = 2.05 \text{ mm}$$

$$C_u = \frac{D_{60}}{D_{10}} = \frac{1.6}{0.7} = 2.3; \quad C_c = \frac{D_{30}^2}{D_{10} \times D_{60}} = \frac{1.2^2}{0.7 \times 1.6} = 1.3$$

From Eq. (2.87), $\phi' = 26 + (10 \times 0.8) + (0.4 \times 2.3) + 1.6\log(1.4) = 35.2^\circ$

b. From Eq. (2.89),
$$a = 2.101 + 0.097 \left(\frac{D_{85}}{D_{15}}\right) = 2.101 + 0.097 \left(\frac{2.05}{0.9}\right) = 2.322$$

From Eq. (2.90), $b = 0.845 - 0.398a = 0.845 - 0.398 \times 2.322 = -0.0792$ From Eq. (2.88),

$$\phi' = \tan^{-1}\left(\frac{1}{ae+b}\right) = \tan^{-1}\left(\frac{1}{2.322 \times 0.61 - 0.0792}\right) = 36.8^{\circ}$$